

$$\frac{d}{dx} \cos x$$

the problem

$$\lim_{h \rightarrow 0} \frac{\cos(x+h) - \cos x}{h}$$

defn of derivative

$$\lim_{h \rightarrow 0} \frac{\cos x \cos h - \sin x \sin h - \cos x}{h}$$

$$\cos(u+v) = \cos u \cos v - \sin u \sin v$$

$$\lim_{h \rightarrow 0} \frac{-\sin x \sin h + \cos x \cos h - \cos x}{h}$$

put terms in order

$$\lim_{h \rightarrow 0} \frac{(\cos x)(\cos h - 1)}{h} + \lim_{h \rightarrow 0} \left( \frac{-\sin x \sin h}{h} \right)$$

$$(ac+bc+d)/q = a(b+c)/q + d/q$$

$$(\cos x) \lim_{h \rightarrow 0} \frac{\cos h - 1}{h} + \lim_{h \rightarrow 0} \left( \frac{-\sin x \sin h}{h} \right)$$

$$\lim(cu) = c \lim u$$

$$(\cos x) \cdot 0 + \lim_{h \rightarrow 0} \left( \frac{-\sin x \sin h}{h} \right)$$

$$\lim_{x \rightarrow 0} \frac{\cos x - 1}{x} = 0$$

$$0 + \lim_{h \rightarrow 0} \left( \frac{-\sin x \sin h}{h} \right)$$

$$x \cdot 0 = 0$$

$$\lim_{h \rightarrow 0} \left( \frac{-\sin x \sin h}{h} \right)$$

$$0+x = x$$

$$-(\sin x) \lim_{h \rightarrow 0} \frac{\sin h}{h}$$

$$\lim(cu) = c \lim u$$

$$-(\sin x) \cdot 1$$

$$\lim_{x \rightarrow 0} \frac{\sin x}{x} = 1$$

$$-\sin x$$

simplify